# PRIIMARY MATHEMATICS 

## Scope and Sequence Grades K - 6

## Scope and Sequence crades K-6

## Kindergarten

Grade I

## Grade 2

## NUMBER AND OPERATIONS

## Sets and Numbers

Use concrete models and pictures to create sets with given numbers of objects to 20. [Chapters I, 2, 3, 6, and 7]

## Number

Representation

Use numbers to represent quantities to
20. [Chapters I, 2, 3, 6, and 7].

Write numerals to represent numbers 0 to 20. [Chapters 2, 3, 5, 6, and 7]

Use concrete and pictorial models to create a set with a given number of objects. (Up to I2O) [Chapters I, 4, and 8] Group objects and numbers up to 120 in tens and ones. [Chapters I, 4, and 8] Use cardinal numbers up to 120 .
[Chapters I, 4, and 8]

Use number bonds to represent number combinations. [Chapters I, 2, 3, and 5]

Use concrete and pictorial models to create a set with a given number of objects. (Up to I,OOO) [Chapter I] Group objects and numbers up to I,OOO into hundreds, tens, and ones. [Chapter I] Group objects into equal sized groups. [Chapter 6]

Use base-ten blocks to create equivalent representations of numbers. [Chapter I]

## NUMBER AND OPERATIONS



## Number

 Representationin different equivalent forms models). [Chapters I, 2, and 4]

## Group objects and numbers

 up toIO million into millions, hundred thousands, ten thousands, thousands, hundreds, tens, and ones. [Chapter I]

Express numbers to 10 million in various forms. [Chapter I] Use exponents to denote powers of IO. [Chapter I]

Understand that positive and negative numbers can be used to describe quantities having opposite directions or values.

## [Chapter 3]

Use positive and negative
numbers to represent
quantities in real-world
contexts. [Chapter 3]
Understand rational numbers
as points on the number line.

## [Chapter 3]

Extend number lines to represent points with negative coordinates; locate negative integers on a horizontal or vertical number line.
[Chapters 3, IO]
Use negative numbers to identify and locate points in all four quadrants of the coordinate plane.

## [Chapter IO]

Understand that the absolute value of a number is its distance from 0 on the number line. [Chapter 3]
Interpret the absolute value of a rational number as magnitude for a positive or negative quantity in a given context. [Chapter 3]

Represent fractions, decimals and integers on a number line.

## [Chapter 3]

Relate the square of a whole number to the area of a square, and the cube of a number to the volume of a cube. [Chapter I] Find the square or cube of a number. [Chapter I]

## Scope cind Sequence crades -6

## Kindergarten

Grade I

## Grade 2

## NUMBER AND OPERATIONS

| Count | Explore count sequence and number <br> names to IOO. [Chapters I, 2, 3, 7, and I2] <br> Count on and back from a given number. <br>  <br>  [Chapters 2, 3, 7, and I2] |
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[Chapters 2, 3, 7, and 12]
Realize that, when counting, the last number named tells how many.
[Chapters I, 2, 3, 7, and I2]
While counting objects, say one number name per item. [Chapters I, 2, 3, 7, and I2] Count numbers of items in sets from different starting points; count sets accurately regardless of arrangements of objects. [Chapters I, 2, 3, 7, and I2] Relate each successive number name to a quantity that is one greater.
[Chapters 2, 3, 7, and I2]
Count up to 20 objects in a set.
[Chapters I, 2, 3, and 7]
Count on to and back from 20. [Chapter 7]
Count by tens to IOO. [Chapter 12]

## Compare and

 Order
## Compose and Decompose

 NumbersCompare and order sets and numbers up to 20 using counting and matching strategies. [Chapter 5]

Count within 120. [Chapters I, 4, and 8] Count by Is and IOs forward and backward to IOO. [Chapters I, 4, and 8]

Compare and order whole numbers to IOO. [Chapters I, 3, 4, 5, 6, and 8] Compare and order using the terms same, more, fewer, greater than, less than, equal to, greatest, and least. [Chapters I, 3, 4, 5, 6, 8, 9, and IO]

Make groups of 10 and count on to tell the number. [Chapters I, 4, and 8]
Use number bonds to add and subtract.
[Chapters 2, 3, 5, and 9]

## Count within I,000. [Chapter I]

Count by multiples of ones, tens, and hundreds. [Chapter I]

Compare and order whole numbers to I,000. [Chapter I]
Use <, >, and = to compare two 2-digit numbers. [Chapter I]

Compose and decompose numbers less than or equal to IO into pairs in more than one way. [Chapter 6]
Compose and decompose numbers less than or equal to 20 into pairs in more than one way. [Chapters 6 and 7]
Compose and decompose numbers from II to 19 into 10 ones and some further ones and 20 as 2 tens. [Chapter 7]

Write multi-digit numbers in expanded form. [Chapter I]



## Scope and Sequence Grades K - 6

| Kindergarten | Grade I | Grade 2 |
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## NUMBER AND OPERATIONS (CONTINUED)

## Place Value

## Fraction

Concepts

Compose and decompose numbers from II to 19 into ten ones and some further ones and 20 as 2 tens. [Chapter 7]
Explore numbers 21 to IOO as tens and ones. [Chapter 12]

Use base-ten blocks and place-value charts to represent numbers to 120 . [Chapters I, 2, 3, 4, 5, 8, and 9]
Write numbers to 120 in standard and word forms. [Chapters I, 4, and 8]

Partition shapes into two to four equal shares. [Chapter II]
Describe the shares using the terms
halves, fourths, and quarters, and use the
phrases half of, fourth of, and quarter of.
[Chapter II]
Understand that dividing a shape into more equal shares makes smaller shares. [Chapter II]

Use place-value models to represent numbers to I,000. [Chapter I] Write numbers to 1,000 in standard, expanded, and word forms. [Chapter I]

Partition circles and rectangles into unit fractions halves, thirds, and fourths.
[Chapter 9]

Identify and relate coin values (penny, nickel, dime, quarter). [Chapter 8]
Count and make simple coin combinations.
[Chapter 8]

Identify $\$ 1, \$ 5, \$ 10, \$ 20$, and $\$ 100$ bills. [Chapter I]
Count and make combinations of coins and bills. [Chapter I]
Compare money amounts. [Chapter I]
Solve word problems involving money,
using $\$$ and $\Phi$ appropriately. [Chapter I]
Use the dollar sign and decimal point.
[Chapter I]

|  | Grade 3 | Grade 4 | Grade 5 | Grade 6 |
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| NUMBER AND OPERATIONS (CONTINUED) |  |  |  |  |
| Place Value | Use place-value models to read, write, and represent numbers to I0,000. <br> [Chapter I] <br> Write numbers to 10,000 in standard, expanded, and word forms. [Chapter I] | Use place-value models to read, write, and represent numbers to I,000,000. <br> [Chapter I] <br> Write numbers to $1,000,000$ in standard, expanded, and word forms. [Chapter I] | Recognize that in a multi-digit number, a digit in one place represents IO times as much as it represents in the place to the right and $\frac{1}{10}$ of what it represents in the place to its left for whole numbers to 10 million. [Chapter I] |  |
| Fraction Concepts | Understand the meanings and uses of fractions including fraction as part of a set. <br> [Chapter 7] <br> Understand that the size of a fractional part is relative to the size of the whole. <br> [Chapter 7] <br> Compare and order fractions using models, and number lines. [Chapter 7] <br> Recognize equivalent fractions through the use of models and number lines. [Chapter 7] <br> Write whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. [Chapter 7] Find a fraction of a set. <br> [Chapter 7] | Recognize, write, name, and illustrate mixed numbers and improper fractions in various forms. [Chapter 6] <br> Generate equivalent fractions. [Chapter 6] <br> Compare nonequivalent fractions by creating common denominators or numerators, or by comparing with benchmark fractions. Use <, >, and = symbols. [Chapter 5] Convert among mixed numbers and improper fractions. <br> [Chapter 6] | Understand how to convert fractions to decimals. <br> [Chapter 4] <br> Understand the relationships between fractions and division expressions. [Chapter 4] |  |
| Money | Add and subtract money. <br> [Chapter 2] <br> Solve real-world problems involving addition and subtraction of money. <br> [Chapter 2] |  |  |  |
| Decimal Concepts |  | Model decimals using tenths and hundredths. <br> Understand decimal notation through hundredths as an extension of the base-ten system. [Chapter 7] <br> Read and write decimals that are greater than or less than I. <br> [Chapter 7] <br> Compare and order decimals. <br> [Chapter 7] <br> Identify equivalent fractions and decimals. [Chapter 7] <br> Use the dollar sign and decimal point in money amounts. <br> [Chapter 7] | Model decimals using thousandths. [Chapter 6] Understand place value concepts through thousandths. [Chapter 6] <br> Understand how to convert decimals to fractions. <br> [Chapter 6] |  |

## Scope and Sequence Grades K - 6

## Kindergarten

Grade I

## Grade 2

## NUMBER AND OPERATIONS (CONTINUED)

Whole Numbe
Computation:
Addition and
Addition and
Subtraction

Whole Number
Computation:
Addition and
Subtraction
Real-World
Problems

Model joining and separating sets.
[Chapters 9, IO, and II]
Use + , - , and $=$ to write number sentences for addition and subtraction stories. [Chapters 9, IO, and II]

Represent and solve addition and subtraction stories with manipulatives, actions, drawings, and number sentences. [Chapters 9, IO, and II]

Practice addition and subtraction in different contexts with words, models, fingers, and numerals. [Chapters 9, 10 , and II]

Model addition and subtraction situations.

## [Chapters 2, 3, 5, 6, and 9]

Add and subtract within 20 , using appropriate models, numbers, and symbols. [Chapters 2, 3, 5, and 6] Understand the meaning of the equal sign; decide if number sentences involving addition and subtraction are true or false.

## [Chapters 2, 3, 5, 6, and 9]

Use the order, grouping, and zero properties to develop addition and subtraction fact strategies.
[Chapters 2, 3, 5, 6, and 9]
Add and subtract up to two 2-digit numbers with and without regrouping.
[Chapters 5, 6, and 9]

Create addition and subtraction stories.
[Chapters 2, 3, 5, 6, and 9]
Solve addition and subtraction problems using basic facts. [Chapters 2, 3, 5, 6, and 9]

Practice addition and subtraction within
IO. [Chapters 2 and 3]

Add the same number to find the total number of items in equal groups.
[Chapter 8]

Model addition and subtraction within I,O00 using place-value strategies.
[Chapters 2 and 3]
Recall addition and subtraction facts. [Chapters 2 and 3]
Use different methods to develop fluency in adding and subtracting multi-digit numbers. [Chapters 2 and 3]
Add and subtract whole numbers to I,000. [Chapters 2 and 3]

Solve multi-digit addition and subtraction problems by using a bar model.
[Chapter 4]

Represent multiplication as repeated addition. [Chapter 6]
Use $\times$ and $=$ symbols to represent multiplication equations. [Chapter 6]

## Grade 3 <br> Grade 4 <br> NUMBER AND OPERATIONS (CONTINUED)

Grade 5
Grade 6

## Whole Number Computation: Addition and Subtraction

Whole Number Computation:
Addition and
Subtraction
Real-World
Problems

## Develop

Fluency with
Addition and Subtraction to 5 or 10

## Whole Number Computation: Multiplication and Division Concepts

Model regrouping in addition and subtraction using placevalue strategies. [Chapter 2] Add and subtract whole numbers to 10,000 .
[Chapter 2]

Model regrouping in addition and subtraction using placevalue strategies. [Chapter 2] Fluently add and subtract multi-digit whole numbers using the standard algorithm. [Chapter 2]

Solve addition and subtraction problems with greater numbers by using a bar model. [Chapter 2]

Model order of operations with whole numbers.
[Chapter 2]

Solve problems using order of operations. [Chapter 2]

Model order of operations with whole numbers.
[Chapter 2]

# Scope and Sequence Grades K - 6 

Kindergarten Grade I Grade 2

## NUMBER AND OPERATIONS (CONTINUED)

## Whole

Number
Computation: Multiplication and Division
Algorithms

## Whole

Number
[Chapter 6]
Computation: Multiplication and Division Real-World Problems

## Fraction

Computation

| Grade 3 | Grade 4 | Grade 5 | Grade 6 |
| :---: | :---: | :---: | :---: |

NUMBER AND OPERATIONS (CONTINUED)
Whole
Number
Computation:
Multiplication
and Division
Algorithms
Whole
Number
Computation:
Multiplication
and Division
Real-World
Problems

## Fraction Computation

Multiply 2-digit numbers by a l-digit number, with and without renaming. [Chapter 4]
Apply properties of addition and multiplication to multiply (partial products). [Chapter 4]

Develop fluency in multiplying multi-digit numbers. [Chapter 3]
Multiply a 4-digit whole number by a l-digit whole number, and multiply two 2-digit numbers using strategies based on place value. [Chapter 3] Divide a 4 -digit number by a I-digit number, with and without a remainder. [Chapters 3 and 4]

Multiply or divide to solve word problems involving multiplicative comparison by using drawings and equations with a symbol for the unknown number to represent the problem. [Chapters 3 and 4]
Solve multi-digit multiplication and division problems.
[Chapters 3 and 4]
Solve division problems that involve interpreting the remainder.

## [Chapters 3 and 4]

Apply understanding of models for multiplication and division.

## [Chapters 3 and 4]

Express a fraction as the sum of repeated unit fractions. [Chapter 7]
Express a whole as the sum of two like fractions. [Chapter 7]

Add and subtract like fractions.
[Chapter 3]
Solve word problems involving multiplication of a fraction by a whole number. [Chapter 3]

Multiply multi-digit numbers.

## [Chapter 2]

Find quotients involving multidigit dividends. [Chapter 2]

## Compare the size of a

 product to one factor without multiplication. [Chapter 2] Solve multiplication and division problems. [Chapter 2] Determine the most useful form of the quotient and interpret the remainder.
## [Chapter 2]

Add and subtract unlike fractions and mixed numbers.

## [Chapter 3]

Multiply proper fractions, improper fractions, mixed numbers, and whole numbers.

## [Chapter 4]

Compare the size of a product
to the size of one factor on the basis of the size of the other
factor, without performing
the indicated multiplication.

## [Chapter 3]

Divide fractions by whole
numbers. [Chapter 4]
Divide a whole number by a
unit fraction. [Chapter 4]
Solve word problems with addition, subtraction,
multiplication, and division of
fractions. [Chapters 3 and 4]

Interpret and compute quotients of fractions.

## [Chapter 2]

Represent situations involving multiplication and division of fractions using models, such as bar models and area models.
[Chapters 2, 4, 5, 6, 8, 9, II, I2] Solve real-world problems involving division of fractions by fractions. [Chapter 2]

## Scope and Sequence Grades K - 6

## Kindergarten <br> Grade I <br> Grade 2

## NUMBER AND OPERATIONS (CONTINUED)

## Decimal Computation

Use mental math strategies to add and subtract. [Chapters 2, 3, and 5]

Solve addition and subtraction word problems involving money. [Chapter I]

Use mental math strategies to add and subtract. [Chapters 2 and 3]

## ALGEBRA / EXPRESSIONS AND EQUATIONS

## Patterns

## Properties

Describe and extend repeating shape patterns. [Chapter 4]
Find missing terms in repeating patterns.
[Chapter 12]
Count by IOs. [Chapter 12]

Identify, describe, and extend two- and three-dimensional shape patterns.

## [Chapter II]

Identify a rule for sorting objects.
[Chapter II]
Identify and extend repeating patterns.
[Chapters 4, 8, and II]
Find missing terms in repeating patterns.
[Chapters 4, 8, and II]
Use the Associative and Commutative
Properties of Addition. [Chapters 2, 5,
and 9]
Additive identity property of 0 . [Chapters 2 ,
5, and 9]

Describe, extend, and create two-dimensional shape patterns.
[Chapter 9]
Skip count by $2 \mathrm{~s}, 5 \mathrm{~s}$, and IOs.
[Chapters I, 2, and 3]
Identify rules for number patterns.
[Chapter I]

Understand that addition and subtraction are inverse operations. [Chapter 3] Use the Associative Property, Identity Property, and Commutative Property as addition strategies. [Chapters 2 and 3]

Determine whether a group of objects has an odd or even number of members. [Chapter 6]
Identify odd and even numbers.
[Chapter 6]

|  | Grade 3 | Grade 4 | Grade 5 | Grade 6 |
| :---: | :---: | :---: | :---: | :---: |
| NUMBER AND OPERATIONS (CONTINUED) |  |  |  |  |
| Decimal Computation | Add and subtract money amounts. [Chapter 2] | Add and subtract money amounts. [Chapter 2] | Model order of operations with decimals. [Chapter 7] | Fluently multiply and divide multi-digit decimals using standard algorithms. <br> [Chapter 2] <br> Represent situations involving multiplication and division of decimals using models, such as bar models and area models. <br> [Chapters 2, 4, 5, 6, 8, 9, II, I2] <br> Solve problems by multiplying and dividing decimals. <br> [Chapters 2, 4, 5, 6, 8, 9, II, I2] |
| Estimation and Mental Math | Use mental math strategies to add, subtract, multiply, and divide. <br> [Chapters 2, 3, 4, and 5] <br> Use mental computation and estimation to assess the reasonableness of answers. [Chapters 2, 3, 4, 5, and 6] Use rounding to estimate sums and differences. [Chapters 2 and 3] | Use mental math and estimation strategies to find sums, differences, products, and quotients. [Chapters I, 2, and 4] <br> Decide whether an estimate or exact answer is needed. <br> [Chapters I, 2, and 4] | Use estimation and mental math to estimate sums, differences, products, and quotients. <br> [Chapters 2 and 6] <br> Round decimals. [Chapter 6] <br> Estimate sums and differences with fractions and decimals. <br> [Chapters 4 and 6] <br> Estimate products and quotients with decimals. <br> [Chapter 6] | Estimate answers to percent problems to check reasonableness. [Chapter 6] |

## ALGEBRA / EXPRESSIONS AND EQUATIONS

Patterns

## Properties

Number Theory

Create and describe addition, Identify, describe, and extend multiplication, and division patterns. [Chapters I, 3, and 4] Skip count by 2 s to 10 s .

## [Chapters 3 and 4]

Analyze number and counting patterns. [Chapters I, 3, and 4]

Understand that multiplication and division are related.
[Chapters 3 and 4]
Create and explain multiplication and division patterns. [Chapters 3 and 4]
Model, define, and explain properties of multiplication. [Chapter 3]
numerical and nonnumerical patterns. [Chapters I and 7] Use a rule to describe a sequence of numbers or objects. [Chapters I and 7]

Understand prime and composite numbers. [Chapter 3]

Find the greatest common factor and least common multiple. [Chapter 3] Determine if a whole number is prime or composite.
[Chapter 3]

Identify, describe, and extend numerical patterns involving all operations. [Chapter 12] Find rules to complete number patterns. [Chapter I2] Form and graph ordered pairs of corresponding terms from two numerical patterns. [Chapter 12]

Explain patterns in the number of zeroes and in the placement of the decimal point when multiplying a number by a power of IO. [Chapter 7]

Apply the least common multiple concept to finding a common denominator for two fractions. [Chapter 4]

Use the distributive property to factor the sum of two whole numbers, or algebraic terms with whole-number coefficients. [Chapter 7]

Write a composite number as a product of its prime factors. [Chapter I]
Find the greatest common factor or least common multiple of two whole numbers. [Chapter I]

## Scope and Sequence Grades K - 6

## Kindergarten <br> Grade I <br> Grade 2

## ALGEBRA / EXPRESSIONS AND EQUATIONS (CONTINUED)

## Functional Relationships

## Expressions/ <br> Models

Use objects, fingers, drawings, and symbols to represent numbers. [Chapters I, 2, 3, 6, 7, and I2] Use a variety of concrete (objects, fingers), pictorial, and symbolic models for addition and subtraction. [Chapters 9, IO, and II]
Use objects to represent geometric figures. [Chapter 4]

Model addition and subtraction stories with addition and subtraction number sentences. [Chapters 9, IO, and II]

Understand the relationships between the numbers in fact families. [Chapters 3 and 5]

Use a variety of concrete, pictorial, and symbolic models for addition and subtraction. [Chapters 2, 3, 5, and 9]

Model addition and subtraction situations by writing addition and subtraction number sentences. [Chapters 2, 3, 5, and 9]

Recognize how bar models show relationships between numbers and unknowns in number sentences. [Chapter 4 ]

Use a variety of concrete, pictorial, and symbolic models for addition, subtraction, and multiplication. [Chapters 2, 3, 4, and 6]

## Number

 Sentencesand Equations

| Grade 3 | Grade 4 | Grade 5 |
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## ALGEBRA / EXPRESSIONS AND EQUATIONS (CONTINUED)

Functional
Relationships
Expressions/
Models

## Number Sentences and Equations

Understand the relationships between the numbers in multiplication-division fact families. [Chapter 4]

Use a variety of concrete, pictorial, and symbolic models for multi-digit addition, subtraction, multiplication, and division. [Chapters 2, 3, and 4] Represent two-step word problems with unknown quantities. [Chapters 2, 3, 4, 6, 8, and 9]

Write addition, subtraction, multiplication, and division equations. [Chapters 2, 3, 4, 6, 8, and 9]
Write and solve equations for one- and two-step real-world problems.
[Chapters 2, 3, 4, 6, 8, and 9]
Determine the missing parts
(quantities or symbols) in equations. [Chapters 2, 3, 4, 6, 8, and 9]

Understand the relationships between the numbers and symbols in formulas for area and perimeter. [Chapter 8]

Use a variety of concrete, pictorial, and symbolic models for the four operations with whole numbers, fractions, and decimals. [Chapters 2, 3, 4, 5, 6, and 7]

Understand the relationships between the numbers and symbols in formulas for volume. [Chapter 9]
Describe number relationships in context. Graph ordered pairs and equations from tables of values. [Chapter II]

Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.
[Chapter 2]
Write and simplify numerical expressions. [Chapter 2]
Evaluate numerical
expressions with two or more operations using the order of operations. [Chapter 2]

Write and solve equations for multi-step word problems.
[Chapters 2 and 3]
Determine the missing parts (quantities or symbols) in equations. [Chapters 2 and 3]

Write and solve equations for multi-step word problems.
[Chapters 2, 3, 5, 8, and II]
Write and solve equations.
[Chapters 2,
3, 5, 8, and II]
Graph linear equations.
[Chapter II]

Use variables to write equations representing two real-world quantities that change in relation to one another. [Chapter 8] Analyze the relationship between an independent and dependent variable using graphs, tables, and equations. [Chapter 8]

Write and evaluate numerical expressions and geometric formulas involving wholenumber exponents. [Chapters

## 7 and 8]

Write and evaluate algebraic expressions using the order of operations. [Chapters 7 and 8] Identify parts of an expression using terms such as sum,
term, product, and coefficient.

## [Chapter 7]

Use the properties of addition and multiplication to write equivalent expressions,
including factoring a common factor from a sum. [Chapters

## 7 and 8]

Identify equivalent expressions and like and unlike terms of an expression. [Chapter 7]
Solve problems using variable expressions in real-world contexts. [Chapters 7 and 8]

Use substitution to identify value(s) that make an equation or inequality true. [Chapter 8]

## Grade 6

## Scope and Sequence Grades K - 6

| Kindergarten | Grade I | Grade 2 |
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## ALGEBRA / EXPRESSIONS AND EQUATIONS (CONTINUED)

## Equality and Inequality

Understand the meaning of the = sign in number sentences. [Chapters 9, IO, and II]

Partition shapes into two to four equal shares. [Chapter II]

Use and create models that demonstrate equality or inequality. [Chapter I]
Use <, >, and = to write equations or inequalities. [Chapter I]

The
Coordinate
Plane


## GEOMETRY

Size and
Position

Use vocabulary such as beside and above to describe and compare relative positions of objects. [Chapter 4]
Use positional words to describe location

Identify and describe two-dimensional shapes in different sizes and orientations.
[Chapter II]

| Grade 3 | Grade 4 | Grade 5 | Grade 6 |
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## ALGEBRA / EXPRESSIONS AND EQUATIONS (CONTINUED)

## Equality and Inequality

## The Coordinate Plane

Use and create models that demonstrate equality or inequality. [Chapter I] Use <, >, and = to write equations or inequalities. [Chapters I and 7]

Understand equality and inequality. [Chapters I, 2, 3, 5, 6, and 7]

Understand equality and inequality. [Chapter I] Write and interpret statements of equality and inequality. [Chapter I]

Identify and plot points in the first quadrant of the coordinate plane. [Chapter II] Make a table of values from an equation, and plot the points these ordered pairs form in the coordinate plane. [Chapter II]

Write and solve addition and multiplication equations to solve real-world problems.

## [Chapter 8]

Write and evaluate an inequality of the form $x<c$ or $x$ $>c$ to represent a real-world situation. [Chapter 8]
Recognize that an inequality of the form $x<c$ or $x>c$ has an infinite number of solutions and represent the solutions on a number line. [Chapter 8]

Use negative numbers to identify and locate points in all four quadrants of the coordinate plane. [Chapter IO] Find the length of horizontal and vertical segments in the coordinate plane. [Chapter IO] Use tables and graphs to represent linear equations.

## [Chapter 8]

Solve real-world problems by graphing points in all four quadrants of the coordinate plane. [Chapter IO]
Plot pairs of equivalent rates represented in the coordinate plane. [Chapter 4]
Draw polygons in the coordinate plane given the coordinates of the vertices.
[Chapter IO]

## GEOMETRY

## Size and <br> Position

## Scope and Sequence Grades K - 6

## Kindergarten

Grade I

## Grade 2

## GEOMETRY (CONTINUED)

## Lines and Angles



## TwoDimensional Shapes / Polygons

## Three-

Dimensional Shapes / Solid Figures

Describe, compare, and name twodimensional shapes regardless of their orientations and overall sizes. [Chapter 4] Name flat shapes that make up surfaces of real-world objects. [Chapter 4] Sort and classify two-dimensional shapes. [Chapter 4]
Combine simple shapes to form larger shapes and pictures. [Chapter 4] Make and extend two-dimensional shape patterns. [Chapter 4]

Analyze, describe, compare, name, and sort solid shapes. [Chapter 4]
Understand that the surfaces of threedimensional shapes are made up of twodimensional shapes. [Chapter 4] Identify, describe, sort, and classify three-dimensional shapes. [Chapter 4] Identify solid figures that slide, stack, and roll. [Chapter 4]

Identify real-world two-dimensional shapes. [Chapter II]
Identify and describe attributes and properties of two-dimensional shapes. [Chapter II]
Sort and classify two-dimensional shapes
based on attributes. [Chapter II]
Compose and decompose two-
dimensional shapes. [Chapter II]

Identify real-world three-dimensional shapes. [Chapter II]
Identify two-dimensional shapes in threedimensional shapes. [Chapter II]
Sort and classify three-dimensional shapes. [Chapter II]
Recognize shapes from different perspectives. [Chapter II]
Compose and decompose threedimensional shapes. [Chapter II]

Recognize and draw shapes based on specified attributes. Identify triangles, quadrilaterals, pentagons, hexagons, and cubes. [Chapter 9]
Identify lines and curves. [Chapter 9]
Compose and decompose two-
dimensional shapes. [Chapter 9]

Identify, describe, sort, and classify three-dimensional shapes. [Chapter 9] Identify solid figures that slide, stack, and roll. [Chapter 9]

## Grade 3

## GEOMETRY (CONTINUED)

| Lines and |
| :--- |
| Angles |
|  |

## Two-

## Dimensional

Shapes / Polygons

Describe, analyze, compare, and classify two-dimensional shapes by their sides and angles. [Chapter II]
Classify and sort polygons and quadrilaterals by specified attributes and properties.
[Chapter II]
Measure and compare the area and perimeter of plane figures in square units. [Chapter 6]

## Three-

Dimensional
Shapes / Solid Figures

Illustrate an angle as an amount of turning. [Chapter II] Name angles. [Chapter II]
Identify right angles and compare angles to right angles. [Chapter II]


Identify perpendicular and parallel lines. [Chapter 9] Estimate before measuring angles [Chapter 9]
Draw perpendicular and parallel lines. [Chapter 9]
Draw and measure angles.

## [Chapter 9]

Understand the relationship between angles and circular measurement $\left(360^{\circ}\right)$.

## [Chapter 9]

Recognize that angle can be broken down into smaller parts. [Chapter 9]
Understand how to work with angles on a straight line.

## [Chapter 9]

Understand how to work with angles at a point. [Chapter 9]
Apply the sum of the angles on a straight line to solve problems. [Chapter 9]

Apply the properties of squares and rectangles.
[Chapters 8 and 9]
Find unknown angle measures and side lengths of squares and rectangles. [Chapters 8 and 9]
Understand the relationships between the numbers and symbols in formulas for area and perimeter. [Chapter 8]

Apply the properties of right, isosceles, and equilateral triangles. [Chapter IO] Apply the properties of a parallelogram, rhombus, and trapezoid. [Chapter IO]

Create a solid figure using unit cubes. [Chapter 9]

Find the lengths of horizontal and vertical segments on a coordinate plane. [Chapter 10]

Identify regular polygons on the coordinate plane.

## [Chapter IO]

Draw polygons in the coordinate plane given the coordinates of the vertices. [Chapter IO]
Use coordinates to find the length of horizontal or vertical sides of polygons. [Chapter 10]

## Scope and Sequence crades -6

## Kindergarten

Grade I

## Grade 2

## GEOMETRY (CONTINUED)

Congruence
and Symmetry

| Coordinate |
| :--- |
| Geometry |
|  |

## Circles

Identify and describe two-dimensional shapes such as circles. [Chapter 4]

Compose two-dimensional shapes such as half-circles and quarter-circles.
[Chapter II]

## MEASUREMENT

## Length and Distance

Compare lengths (long, short, longer, shorter). [Chapter 8]
Describe and compare lengths and heights using nonstandard units.

## [Chapter 8]

Develop a background for measurement by comparing and using nonstandard units. [Chapter 8]

Compare the lengths of two objects
by comparing each with a third length
(transitivity). [Chapter 7]
Use a start line to measure length.

## [Chapter 7]

Measure lengths using nonstandard units.

## [Chapter 7]

Explain the need for equal-length units to measure. [Chapter 7]
Count length units in groups of tens and ones. [Chapter 7]
Compare measurements made using different units. [Chapter 7]
Understand the inverse relationship
between the size of a unit and the number
of units. [Chapter 7]

Demonstrate linear measure as an iteration of units. [Chapter 5]
Use rulers to measure length. [Chapter 5]
Estimate and measure length. [Chapter 5] Measure length in meters, centimeters,
feet, and inches. [Chapter 5]
Use units of different length to measure an object twice; describe how the two measurements relate to the size of the unit chosen. [Chapter 5]
Compare and measure lengths using customary and metric units. [Chapter 5] Demonstrate partitioning and transitivity in relation to length. [Chapter 5] Solve problems involving estimating, measuring, and computing length.

## [Chapter 5]

Solve addition and subtraction word problems involving length. [Chapter 5]

| Grade 3 | Grade 4 | Grade 5 | Grade 6 |
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## GEOMETRY (CONTINUED)

| Congruence and Symmetry | Recognize line symmetry. <br> [Chapter 9] |  |
| :---: | :---: | :---: |
| Coordinate Geometry |  | Develop coordinate readiness with tables and line graphs. <br> [Chapter II] <br> Plot points on a coordinate grid (first quadrant only). <br> [Chapter II] |
| Circles | Understand the relationship between angles and circular measurement (360 $)$. <br> [Chapter 9] |  |
| MEASURE |  |  |

## Length and Distance

Solve real-world problems in measurement. [Chapters 2, 3, and 4]

## Convert from larger to smaller

 customary units of length.[Chapters IO and II]
Convert from larger to
smaller metric units of length.
[Chapters IO and II]
Solve real-world problems
involving length. [Chapters IO and II]

Use measurement conversions of length in solving real-world problems.
[Chapters I, 2, 3, and 8]

## Weight/Mass

Select appropriate units and tools to estimate and measure masses of objects in kilograms or grams. [Chapter 8]
Compare masses in kilograms or grams. [Chapter 8] Solve addition, subtraction, multiplication, or division word problems involving mass in kilograms or grams.

Convert from larger to smaller customary units of weight/ mass. [Chapters IO and II] Convert from larger to smaller metric units of weight/mass.

## [Chapters IO and II]

Solve real-world problems involving weight/mass.
[Chapters IO and II]

Use measurement conversions of weight/mass in solving realworld problems. [Chapters I,
2, 3, and 8]
[Chapter 8]

# Scope and Sequence Grades K - 6 

| Kindergarten | Grade I | Grade 2 |
| :---: | :---: | :---: |

## Capacity/ <br> Volume

## Time

## Angles

Tell time to the hour and half-hour on analog and digital clocks. [Chapter 12] Estimate time to the hour or half-hour. [Chapter I2]

Tell and write time using A.M. and P.M. [Chapter 7]
Tell time to five minutes. [Chapter 7] Identify elapsed time of one hour or half hour. [Chapter 7]

Recognize and draw shapes given a number of angles. [Chapter 9]

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| :--- | :--- | :--- | :--- |

## MEASUREMENT (CONTINUED)

Capacity/
Volume
Time
Angles

Compare angles to right angles.
[Chapter II]
Select appropriate tools and units to estimate and measure volume and capacity in liters.

## [Chapter 9]

Compare volume or capacity in liters. [Chapter 9]
Solve addition, subtraction, multiplication, or division word problems involving volume or capacity in liters. [Chapter 9]

Tell time to the minute.

## [Chapter 5]

Convert between hours and
minutes. [Chapter 5]
Determine elapsed time, start
time, and end time. [Chapter 5]
Add and subtract units of time.
[Chapter 5]

Perimeter

Convert from larger to smaller
customary units of capacity.
[Chapters IO and II]
Convert from larger to smaller
metric units of capacity.
[Chapters IO and II]
Solve real-world problems involving capacity. [Chapters IO and II]

Use measurement conversions of capacity/volume in solving real-world problems. Estimate and measure volume in cubic units. [Chapter 9]
Recognize volume as additive and find the volumes of prisms and solid figures. [Chapter 9] Use formulas to find the volume of rectangular prisms and other solid figures.
[Chapter 9]

Estimate and measure angles in whole-number degrees with a protractor. [Chapter 9] Classify angles by angle measure and recognize angle measure as additive.

## [Chapter 9]

Relate $\frac{1}{4}-, \frac{1}{2}-, \frac{3}{4}-$, and full turns to the number of right angles. [Chapter 9]
Understand the relationship between angles and the 360 degrees of the measure of a circle. [Chapter 9]
Apply the idea that the sum of angles on a straight line is $180^{\circ}$. [Chapter 9]
Apply the idea that vertical angles are equal in measure.

## [Chapter 9]

Apply the idea that the sum of angles at a point is $360^{\circ}$.

## [Chapter 9]

Find the perimeter of squares, rectangles, and composite figures. [Chapter 8]
Solve problems involving the perimeter of squares, rectangles, and composite figures. [Chapter 8]

Measure perimeter of plane figures. [Chapter 6]
Choose the appropriate tool, unit, and strategy to measure perimeter.
[Chapter 6]

# Scope and Sequence Grades K - 6 

| Kindergarten | Grade I | Grade 2 |
| :---: | :---: | :---: |

Compose and decompose twodimensional shapes (foundation for understanding area). [Chapter II]

Develop foundations for understanding

## MEASUREMENT (CONTINUED)

## Surface Area and Volume

Area

|  | Grade 3 | Grade 4 | Grade 5 | Grade 6 |
| :---: | :---: | :---: | :---: | :---: |
| MEASUREMENT (CONTINUED) |  |  |  |  |
| Area | Find and compare the area of plane figures in different square units. <br> [Chapter 9] <br> Draw different plane figures with the same area. [Chapter 9] <br> Estimate area of small and large surfaces. <br> Compare the area and perimeter of two plane figures. [Chapter 9] Find the area of rectangles and composite figures. [Chapter 9] | Connect area measure to the area model for multiplication; use it to justify the formula for the area of a rectangle. [Chapter 8] Estimate and measure area in square units. [Chapter 8] Select appropriate units, strategies, and tools to solve area. [Chapter 8] Recognize area as additive. [Chapter 8] <br> Solve problems involving the area of squares, rectangles, and composite figures. [Chapter 8] |  | Find the area of triangles, parallelograms, trapezoids, and regular polygons by decomposing into rectangles or triangles. [Chapter 9] Find a missing dimension of a plane figure given its area and other dimension(s). [Chapter 9] Solve real-world problems involving the areas of triangles, parallelograms, trapezoids, and regular polygons. [Chapter 9] |
| Surface Area and Volume |  |  | Estimate and measure volume in cubic units. [Chapter 9] | Represent prisms and pyramids with triangular or rectangular faces using nets. [Chapter II] <br> Use nets of prisms and pyramids to find the surface areas. [Chapter II] Find the volume of a rectangular prism with fractional edge lengths, and relate this to the formula V =Lwh. [Chapter II] Find the volume of prisms using the formulas $\mathrm{V}=\mathrm{Bh}$. [Chapter II] Solve real-world problems involving surface area and volume of prisms. [Chapter II] |

## RATIOS AND PROPORTIONAL RELATIONSHIPS

## Ratios

Understand the concept of ratio and use ratio language to describe proportional relationships. [Chapter 4] Find the missing term in a pair of equivalent ratios or in a ratio table. [Chapter 4] Plot pairs of equivalent rates in the coordinate plane.
[Chapter 4]
Use tables to compare ratios.

## [Chapter 4]

Solve multi-step real-world problems involving ratios using bar models. [Chapter 4]

## Scope and Sequence Grades K - 6

## Kindergarten

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## RATIOS AND PROPORTIONAL RELATIONSHIPS (CONTINUED)

```
Representing
Ratios
```


## Rates

## Percents

## DATA ANALYSIS / STATISTICS AND PROBABILITY

Classifying and Sorting

Understand similarities and differences in objects and shapes. [Chapter 4]
Identify attributes that may be used as a basis for sorting. [Chapter 4]
Sort and classify objects using one or two attributes. [Chapter 4 ]
Count and compare numbers of objects in categories. [Chapter 5]

Sort and classify two- and threedimensional shapes by properties.
[Chapter 9]
Collect and organize data and represent
it in different ways. [Chapter 8]

Collect and organize data in different
ways. [Chapter IO]

Collect and organize data in different ways. [Chapter 8]

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| :---: | :---: | :---: | :---: |
| RATIOS AND PROPORTIONAL RELATIONSHIPS (CONTINUED) |  |  |  |


| Representing |
| :--- |
| Ratios |
|  |
|  |
|  |

Use multiplication or division to write equivalent ratios.
[Chapter 4]
Make tables of equivalent ratios. [Chapter 4]
Use bar models to solve problems involving ratios of three quantities. [Chapter 4]

Understand the concept of a unit rate $a / b$ associated with a ratio $a: b(b \neq 0)$, and use rate language in proportional situations. [Chapter 5] Compute and compare unit rates using the division algorithm. [Chapter 5] Solve unit rate problems, including unit pricing and constant speed.
[Chapter 5]
Solve percent problems involving simple interest, tax, markups, discounts, and commissions. [Chapter 6]
Convert fractions to percents.
[Chapter 6]
Find a percent of a number.
[Chapter 6]

## DATA ANALYSIS / STATISTICS AND PROBABILITY

| Classifying and Sorting | Classify and sort polygons and quadrilaterals by specified attributes and properties. <br> [Chapter II] <br> Collect and organize data and represent it in different ways. <br> [Chapter IO] | Construct line plots. [Chapter 6] | Represent data in frequency tables, dot plots and histograms. [Chapter 12] Display a data set in a box plot. [Chapter 12] |
| :---: | :---: | :---: | :---: |
| Collect and Organize Data | Collect and organize data and represent it in different ways. <br> [Chapter IO] |  |  |

## Scope and Sequence Grades K - 6

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DATA ANALYSIS / STATISTICS AND PROBABILITY (CONTINUED)

Represent Data

## Interpret/ Analyze Data

Represent data in picture graphs and tally charts. [Chapter IO]

Interpret data in picture graphs and tally charts. [Chapter IO]
Solve problems involving data.
[Chapter IO]

Represent measurement data in a line plot using whole numbers. [Chapter 8]

Solve problem situations using graphs.
[Chapter 8]

## MAKING SENSE IN SOLVING PROBLEMS

Build Skills
Through
Problem
Solving

Solve RealWorld Problems

Build skills in comparing sets, and addition and subtraction encountering, discussing, and solving problems.

Build skills in addition, subtraction, and measurement through problem solving.

Solve real-world problems involving addition and subtraction.
Determine coins needed for various purchases.

Build skills in addition, subtraction, multiplication, and measurement through problem solving.

Solve real-world problems involving addition, subtraction, multiplication, and measurement.

## Grade 3

Grade 4
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Grade 6
DATA ANALYSIS / STATISTICS AND PROBABILITY (CONTINUED)

Represent Data

Interpret/ Analyze Data

Represent measurement data in a line plot where the horizontal scale is marked in whole numbers, halves, or quarters. [Chapter IO]

Interpret picture graphs and bar graphs with scales. [Chapter IO]
Use bar graphs, picture graphs, and line plots to solve real-world problems. [Chapter IO]

Make a line plot to display a data set of measurements in fractions of a unit. [Chapter 6]

Interpret line plots.<br>[Chapter 6]

Make a line plot to display a data set of measurements in fractions of a unit. [Chapter 7]

Interpret line graphs and line plots. [Chapter II]
Interpret a line plot to solve problems involving addition, subtraction, multiplication, and division of fractions.
[Chapter II]

Recognize a statistical question.

## [Chapter I2]

Understand that a data set
has a distribution, which can be described by its center and shape. [Chapter I2]
Recognize that a measure of center summarizes all values of a data set with a single number.
[Chapter 12]
Identify measures of center of a data set and calculate each, and know when each is most useful.

## [Chapter 12]

Describe the overall shape of a distribution, and relate the choice of a center to the shape of the distribution. [Chapter 12] Solve real-world problems involving the mean or median, such as finding a missing data value given the mean.
[Chapter 12]
Compute measures of variability for a data set: quartiles, interquartile range and mean absolution deviation. [Chapter 12]

## MAKING SENSE IN SOLVING PROBLEMS

## Build Skills Through Problem <br> Solving

## Solve RealWorld <br> Problems

Build skills in addition, subtraction, multiplication, division, and measurement through problem solving.

Solve real-world problems involving addition, subtraction, multiplication, division, and measurement.

Build skills in multiplication, division, fraction concepts, data analysis, and measurement through problem solving.

Solve real-world problems involving addition, subtraction, multiplication, division, and measurement.

Build skills in multiplication, division, fraction concepts, decimals, geometry, data analysis, and measurement through problem solving.

Solve real-world problems involving multiplication, division, concepts with whole numbers, fractions, and decimals, data analysis, and measurement.

Build skills in multiplication and division of fractions and decimals, ratios, and percents; algebra, data analysis, and geometry and measurement through problem-solving.

Solve real-world problems involving multiplication, division, concepts with fractions,
decimals, ratios, and percents; data analysis, geometry, and measurement.

## Scope and Sequence Grades K - 6

## Kindergarten

Grade I
Grade 2

## MAKING SENSE IN SOLVING PROBLEMS (CONTINUED)

## Use

Appropriate Strategies and Thinking Skills to Solve Problems

## Apply and

 Explain Problem SolvingDecide on number sentences to fit addition and subtraction situations.

Solve real-world problems and describe methods for doing so.
Explain why solutions make sense and are correct.

Apply problem-solving strategies in Think! and Problem Solving activities.

Apply and explain problem-solving processes in Think! and other activities.

Apply problem-solving strategies in Think! and Problem Solving activities.

Apply and explain problem-solving processes in Think! and other activities.

## REASONING

| Explore |
| :--- |
| Concepts |
|  |
|  |

## Investigate

 Mathematical Ideas
## Identify,

Demonstrate, and Express Regularity in Reasoning

Use models to explain reasoning.

Apply counting and comparing skills in a wide variety of contexts; use numerals to convey information.
Investigate ideas with two- and threedimensional shapes.
Investigate measurement concepts.

Explain ways of identifying equal sets or explain which set has more or fewer. Use a balance to determine weights of objects in nonstandard units. Demonstrate that only a few big objects fit into small spaces and many small objects fit into big spaces. Describe, sort, and classify two- and three-dimensional shapes.
Interpret data in tally charts and bar graphs.
Identify and extend repeating shape patterns.

Explore concepts more deeply and justify reasoning.
Apply thinking skills in Think! and Problem Solving activities.

Further investigate mathematical ideas by completing critical thinking skills activities.

Explore transitivity by comparing lengths of three different objects.
Identify and describe attributes and properties of two- and three-dimensional shapes.
Interpret picture graphs, tally charts, and bar graphs.
Identify and extend growing number patterns and repeating shape patterns.

Explore concepts more deeply and justify reasoning in Think!, Math Talk, and Activities.
Apply thinking skills in Think!, Math Talk, Heuristics, and problem solving.

Further investigate mathematical ideas by completing critical thinking skills activities.

Demonstrate the inverse relationship between the size of a unit and the number of units.
Identify, describe, sort, and classify two- and three-dimensional shapes. Identify rules for number patterns. Explain why solutions make sense and are correct.
Resist counter-suggestions about answers.

## Grade 3 Grade $4 \quad$ Grade $5 \quad$ Grade 6

## MAKING SENSE IN SOLVING PROBLEMS (CONTINUED)

## Use <br> Appropriate Strategies and Thinking Skills to Solve Problems <br> Apply and Explain Problem Solving

Apply problem-solving strategies in Think! and Problem Solving activities.

Apply and explain problemsolving processes in Think! and other activities.

Use appropriate strategies to solve real-world problems.

Apply and explain problemsolving processes in Think! and other activities.

Use appropriate strategies to solve real-world problems.

Apply and explain problemsolving processes in Think! and other activities.

Discuss mathematical ideas use appropriate strategies, solve real-world problems, and explain solution methods in class.

Apply and explain problemsolving processes in Think! and other activities.

## REASONING

Explore
Concepts

Investigate Mathematical Ideas

Identify,
Demonstrate, and Express
Regularity in
Reasoning

Explore concepts more deeply and justify reasoning in Think!, Math Talk, and Activities. Apply thinking skills in Think!, Math Talk, Heuristics, and problem solving

Further investigate mathematical ideas by completing critical thinking skills activities.

Classify and identify twodimensional shapes as polygons.
Interpret picture and bar graphs with scales and line plots.
Create and explain multiplication and division patterns.
Explain why solutions make sense and correct.

Resist counter-suggestions about answers.

Explore concepts more deeply and justify reasoning in Think!, Math Talk, and Activities. Apply thinking skills in Think!, Math Talk, Heuristics, and problem solving.

Further investigate mathematical ideas by completing critical thinking skills activities.

Demonstrate the relationship between fractions on a number line and rulers marked with halves and fourths of an inch.
Analyze line plots with fractions of a unit.
Identify, describe, and extend numerical and nonnumerical patterns.
Explain why solutions make sense and are correct.
Resist counter-suggestions about answers.

Explore concepts more deeply and justify reasoning in Think!, Math Talk, and Activities Apply thinking skills in Think!, Math Talk, Heuristics, and problem solving.

Further investigate mathematical ideas by completing critical thinking skills activities.

Use properties of squares and rectangles to solve problems. Use properties of triangles and four-sided figures to solve problems.

Make and analyze a line plot to represent a data set of measurements in fractions of a unit.
Identify, describe, and extend numerical patterns involving all operations.
Explain why solutions make sense and are correct.

Resist counter-suggestions about answers.

Explore concepts more deeply and justify reasoning in Think!, Math Talk and Activities. Apply thinking skills in Think!, Math Talk, Heuristics and problem solving

Further investigate mathematical ideas by completing critical thinking skills activities.

Continue to use bar models to solve real-world problems involving multiplication, division, concepts with fractions,
decimals, ratios, and percents; data analysis, geometry and measurement.
Apply the properties of operations to generate equivalent numerical and algebraic expressions.
Apply standard algorithms for addition, subtraction, multiplication, and division of whole numbers and decimals. Apply standard algorithms for multiplication and division with fractions.
Apply concept of prime factorization to finding square roots and cube roots of perfect squares and perfect cubes.

## Scope and Sequence Grades K - 6

## Kindergarten

Grade I
Grade 2

## REASONING (CONTINUED)

Use a Variety of Reasoning Skills

Sort and classify using attributes. Identify similarities and differences. Determine numbers given clues; explain and justify answers.
Analyze two- and three-dimensional shapes; identify their attributes and name them based on their attributes.

Recognize shapes from different perspectives.
Use the Commutative and Associative properties, and tens and ones to solve two-digit addition and subtraction problems.

Identify solid figures that slide, stack, and roll.
Explore the inverse relationship between addition and subtraction.

## COMMUNICATION

Consolidate
Mathematical
Thinking

Consolidate thinking in independent

## Communicate with Peers, <br> Teachers, and Others <br> Share <br> Mathematical <br> Thinking

Construct
Arguments and Express Mathematics
Ideas
activities.

Discuss mathematical ideas in paired and small group activities as well as activities led by the teacher.

Share mathematical ideas in paired and small group activities.

Express ideas with words and gestures - in paired and small group activities as well as activities led by the teacher. Use models and pictures as stimuli for explaining thinking.

## Present mathematical thinking through

 Math Talk and Think!Discuss mathematical ideas in Math Talk Think!, Activities, and STEAM Project work.

Share mathematical ideas in paired and small group activities.

Express ideas in Think! and Math Talk, and some tasks in Practice On Your Own.

Present mathematical thinking through Math Talk and Think!

Discuss mathematical ideas in Math Talk, Think!, Activities, and STEAM Project work.

Share mathematical ideas in paired and small group activities.

Express ideas in Think! and Math Talk, and some tasks in Practice On Your Own.

## CONNECTIONS AND STRUCTURE

Look for and
Use Structure to Recognize Connections in Mathematical
Ideas

Understand the connection between quantities and written numerals.
Use numbers to describe properties of geometric shapes.
Use counting and numbers while measuring in nonstandard units.

## Relate counting to addition and

 subtraction.Understand the relationships between the numbers in fact families.
Connect addition and multiplication (repeated addition).
Recognize and apply different strategies for adding and subtracting I- and 2-digit numbers.

## Examine and apply the inverse

 relationship between addition and subtraction.Connect geometric concepts with unit fractions of halves and fourths.

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## REASONING (CONTINUED)

## Use a Variety of Reasoning Skills

Model, define, and explain properties of multiplication. Explore the inverse relationship between multiplication and division. Use estimation to check reasonableness

Use properties of squares and rectangles to solve problems about area and perimeter. Explore the relationship between models for multiplication and division for whole numbers.

Use estimation to check reasonableness (wholenumber addition, subtraction, multiplication, and division).

Use properties to classify triangles and quadrilaterals. Apply understanding of models for multiplication and division of fractions and decimals by whole numbers.
Use number properties (including the distributive property) to check reasonableness of results.

Develop and apply formulas for finding the area of triangles, parallelograms, trapezoids, and regular polygons.
Develop and apply other formulas such as the distance formula.

## COMMUNICATION

Consolidate
Mathematical
Thinking

Present mathematical thinking through Math Talk and Think!

Present mathematical thinking through Math Talk and Think!

Discuss mathematical ideas in Math Talk, Think!, Activities, and STEAM Project Work.

Share mathematical ideas in paired and small group activities.

Express ideas in Think! and Math Talk, and some tasks in Practice On Your Own.

Present mathematical thinking through Math Talk and Think!

Discuss mathematical ideas in Math Talk, Think!, Activities, and STEAM Project Work.

Share mathematical ideas in paired and small group activities.

Express ideas in Think! and Math Talk, and some tasks in Practice On Your Own.

Present mathematical thinking through Math Talk and Think!

Discuss mathematical ideas in Math Talk, Think, Activities, and STEAM Project Work.

Share mathematical ideas in paired and small group activities.

Express ideas in Think! and Math Talk and some tasks in Practice on Your Own.

## CONNECTIONS AND STRUCTURE

Look for and
Use Structure to Recognize Connections in Mathematical Ideas

[^0] between the numbers in multiplication-division fact families.

Understand the relationship between fractions and division. Understand the relationship among fractions, and decimals, as ways to represent parts of a whole.
Understand the relationship between fractions and division. Convert among mixed numbers and improper fractions.

Relate ratios, fractions, and rates.

Understand that ratios can represent part-to-part as well as part-to-whole relationships.
Convert among fractions, decimals, and percents.

## Scope and Sequence Grades K - 6

## Kindergarten

Grade I

## Grade 2

## CONNECTIONS AND STRUCTURE (CONTINUED)



Understand How Concepts Build on One Another

Solve Real-
World
Problems
in Contexts
Outside of Mathematics

Understand the connection between quantities and written numerals. Use numbers to describe properties of geometric shapes.
Use counting and numbers while measuring in nonstandard units.

Explore relationships among counting, ordering, and ordinal numbers. Compare and relate attributes of twoand three-dimensional figures.
Use a variety of measurement attributes to compare objects.

Solve real-world problems involving more and less, addition, and subtraction. Identify two- and three-dimensional figures in real-world objects.

Relate counting to addition and subtraction.
Understand the relationships between the numbers in fact families.
Connect addition and multiplication (repeated addition).
Recognize and apply different strategies for adding and subtracting I- and 2-digit numbers.

Examine and apply the inverse relationship between addition and subtraction.
Connect geometric concepts with unit fractions of halves and fourths.

Learn how place-value concepts apply to regrouping in addition and subtraction.

Solve real-world problems involving addition, subtraction, graphs, and money.

Understand how patterns can be described using numbers, operations, and data displays.
Recognize the relationship between bar models, number sentences, and number patterns.

Solve real-world problems involving addition, subtraction, measurement, and data analysis.

## Grade 3

Grade 4

## Grade 6

## CONNECTIONS AND STRUCTURE (CONTINUED)



## Understand

 How Concepts Build on One AnotherSolve Real-
World
Problems
in Contexts
Outside of Mathematics

Apply the inverse relationship between multiplication and division.
Understand that the size of a fractional part is relative to the size of the whole. Connect subtraction and division (repeated subtraction). Recognize and apply different strategies for multiplication and division facts.
Understand the relationships between the numbers in multiplication-division fact families.

Understand the meanings and uses of fractions including fraction of a set.
Use addition, subtraction, multiplication, and division to construct and analyze graphs and line plots.

Solve real-world problems involving addition, subtraction, multiplication, division, and measurement.
Solve real-world problems related to money.

## Demonstrate that decimal

 notation is an extension of the base-ten system. Examine the relationship between fractions and decimals.Make connections among multiplication, division, factors, and multiples.
Connect the units of
customary capacity to one another.

Describe number relationships in context.
Identify equivalent fractions and decimals.
Make connections among the greatest common factor, least common multiple, and operations with fractions.

Solve real-world problems involving multiplication, division, fraction concepts, data analysis, and measurement.

Understand the relationship between fractions and division. Understand the relationship among fractions, and decimals, as ways to represent parts of a whole.
Understand the relationship between fractions and division. Convert among mixed numbers and improper fractions.

Identify equivalent fractions, mixed numbers, and decimals. Make connections among operations with fractions and decimals.

Solve real-world problems involving multiplication, division, fraction, decimal, ratio, and percent concepts; data analysis, and measurement.
Solve real-world problems involving all four operations with whole numbers, fractions, and decimals; algebra, geometry, measurement, and data analysis.

Relate ratios, fractions, and rates.
Understand that ratios can represent part-to-part as well as part-to-whole relationships.
Convert among fractions, decimals, and percents.

Make connections between ratios, fractions, and rates. Make connections between squares and square roots, cubes and cube roots.

Solve real-world problems involving multiplication, division, concepts with fractions, decimals, ratios and percents; data analysis, geometry, and measurement.

## Scope and Sequence Grades K - 6

## Kindergarten

Grade I

## Grade 2

## REPRESENTING AND MODELING MATHEMATICS

## Use <br> Representations <br> to Attend to <br> Precision

Use concrete models to create a set with a given number of objects to 20 .
Use numbers to represent quantities up to 20.
Use picture cards to communicate understanding of comparisons (bigger, taller, smaller).
Understand the meaning of the,+- , and $=$ symbols in number sentences.
Model addition and subtraction stories with addition and subtraction number sentences.
Represent addition and subtraction stories.

Use concrete and pictorial models to create a set with a given number of objects. (Up to I20)
Represent numbers to IOO on a number line.
Use number bonds to represent numbers. Understand equality and inequality. Use the,+- , and = symbols to represent real-world addition and subtraction situations.
Represent numerical data using picture graphs, tally charts, and bar graphs.
Represent sharing equally and making equal groups.
Identify, describe, and extend two- and three-dimensional shape patterns.
Identify a rule for sorting objects.
Identify and extend repeating patterns.

Use concrete and pictorial models to create a set with a given number of objects. (Up to I,OOO)
Represent numbers to $\mathrm{I}, \mathrm{OOO}$ on a number line.
Use symbolic notation (<, >) to compare numbers.
Use bar models to represent addition and subtraction situations.
Represent numerical data using picture graphs, tally charts, bar graphs, and line plots.
Use the $\times, \div$, and $=$ symbols to represent multiplication situations.
Represent division as repeated subtraction equations.
Describe, extend, and create two-dimensional shape patterns. Identify rules for number patterns.

## Grade 3 <br> Grade 4 <br> Grade 5 <br> Grade 6

## REPRESENTING AND MODELING MATHEMATICS

## Use <br> Representations <br> to Attend to <br> Precision

Use place-value models to read, Represent numbers to I million write, and represent numbers to 10,000.
Represent numbers in different equivalent forms.
Use the dollar sign and decimal point in money amounts.
Solve addition and subtraction problems with greater numbers by using a bar model.
Use the $\times, \div$, and $=$ symbols to represent multiplication and division situations.

Use a variety of representations for multiplication and division, such as skip counting, repeated addition or subtraction, arrays, area models, number lines, grouping, and sharing.
Determine the missing parts (quantities or symbols) in equations.
Create and analyze
multiplication and division patterns.
Identify a rule for number and counting patterns.
in various contexts
Write numbers to I million in standard, expanded, and word forms.
Model decimals to tenths and hundredths.
Write addition and subtraction equations for real-world problems with fractions and decimals.
Define and use symbols in geometry to identify and relate geometric figures. Use a variety of models to represent multi-step realworld problems with whole numbers, fractions, and decimals.
Use geometry tools (protractor, set squares, grid paper) to model problems.
Use a rule to describe a sequence of numbers or objects.
Understand the relationships
between the numbers and
symbols in formulas for area and volume.

Write numbers to 10 million in various forms.
Model decimals to thousandths. Use letters as variables to represent unknown values in equations and formulas.
Convert fractions and mixed numbers to decimals and decimals to fractions and mixed numbers.
Interpret symbols of relation in comparing whole numbers, fractions, and decimals.
Use a variety of models for multiplication and division of fractions and decimals by whole numbers.
Use the order of operations in numeric expressions with two or more operations and grouping symbols.
Write and solve equations.
Use a coordinate grid to
represent an equation as a graphed line.
Find rules to complete number patterns.

Translate between fractions, decimals, ratios, and percents. Select the most useful form (fraction or decimal) for solving problems involving percents.
Use a variety of models to solve problems involving ratios, rates, and percents. Use visual models (area models, sets, and number line drawings) to represent problems involving fractions, decimals, ratios, rates, and percents.
Use part/whole, comparison, and before and after bar models to represent multistep real-world problems with whole numbers, fractions decimals, ratios, rates, and percents.
Measure distances in the coordinate plane.
Use nets to find the surface areas of pyramids and prisms. Represent data in dot plots and histograms.
Display numerical data in plots on a number line, including
line plots, dot plots, and histograms.

## Scope and Sequence Grades K - 6

## Kindergarten

Grade I

## Grade 2

## REPRESENTING AND MODELING MATHEMATICS (CONTINUED)

## Select

 and Apply Appropriate Models and Tools toRepresent
Problems

## Interpret

Phenomena Through Representations

Represent quantities with objects, number cubes, fingers, pictures/drawings, number cards, acting out, tallies, and numerals.

Use number bonds to represent number combinations.
Use a variety of concrete, pictorial, and symbolic models and tools for addition and subtraction.
Use technology (virtual manipulatives and computers) to model and draw.

Measure and compare lengths and weights using nonstandard units. Identify real-world two- and threedimensional shapes.
Represent data in picture graphs.
Use a variety of models for adding and subtracting.

Use place value models to create equivalent representations of numbers. Use a variety of concrete, pictorial, and symbolic models and tools for addition, subtraction, and multiplication.
Represent multiplication with skip counting and arrays.
Use customary and metric measuring tools to measure length.
Use technology (virtual manipulatives and computers) to model and draw.

Use metric and customary units to measure length to the nearest unit. Represent data in bar graphs and picture graphs.
Solve real-world problems about social phenomena.
Use bar models to represent addition and subtraction situations.

## Grade 3

Grade 4
Grade 5

## Grade 6

## REPRESENTING AND MODELING MATHEMATICS (CONTINUED)

Select
and Apply
Appropriate
Models and
Tools to
Represent
Problems

Interpret Phenomena Through Representations

Use a variety of concrete, pictorial, and symbolic models and tools for multidigit addition, subtraction, multiplication, and division. Represent multiplication with skip counting and arrays. Use a variety of models to represent fractions and equivalent fractions. Use technology (virtual manipulatives and computers) to model and draw.

Solve problems about sharing equally and making equal groups.
Use metric units to measure mass and volume to the nearest unit.
Use referents to estimate mass and volume.
Use bar models to represent addition, subtraction, and multiplication situations.
Solve problems about sharing equally and making equal groups.
Use bar graphs, picture graphs, and line plots to solve problems.
Represent measurement data using a line plot where the horizontal scale is marked in whole numbers, halves, or quarters.
Solve real-world problems involving social situations. Solve real-world problems related to money.

Use a variety of models for multi-digit multiplication and division of whole numbers. Use technology (virtual manipulatives and computers) to model and draw.
Use customary measuring tools to measure length, weight, and capacity.

Measure perimeter and area in customary and metric units. Collect data and organize it in a table.
Create a line graph from data in a table.
Interpret a line plot to solve problems involving addition and subtraction of fractions. Solve real-world problems involving multiplication, division, fraction concepts, data analysis, and measurement.

Translate between equivalent improper fractions and mixed numbers.
Translate among fractions, mixed numbers, and decimals. Find the most useful form of a quotient.
Use a variety of models and
tools for multiplication and division of fractions and decimals by whole numbers. Use technology (virtual manipulatives and computers) to model and draw.

Measure volume of a rectangular prism. Generate a line plot to represent measurement data. Make a table of values from an equation, and plot the points these ordered pairs form in the coordinate plane. Solve real-world problems involving whole number, fraction, and decimal operations, algebra, data analysis, and measurement.

Use geometry tools (protractor, set squares, grid paper) to model problems. Use technology (virtual manipulatives and computers) to model and draw.
Select appropriate formulas and units in solving problems involving perimeter, area, surface area, and volume. Use a calculator to model, compute, and solve.

Write the square and cube of a whole number using indices. Represent negative numbers on a number line and in the coordinate plane.
Represent solutions of inequalities on a number line. Understand absolute value of a rational number as its distance from 0 on a number line.
Find equivalent ratios and rates.


[^0]:    Apply the inverse relationship between multiplication and division.
    Understand that the size of a fractional part is relative to the size of the whole. Connect subtraction and division (repeated subtraction). Recognize and apply different strategies for multiplication and division facts.
    Understand the relationships

    Demonstrate that decimal notation is an extension of the base-ten system.
    Examine the relationship between fractions and decimals.
    Make connections among multiplication, division, factors, and multiples.
    Connect the units of customary capacity to one another.

